

The math concepts and skills learned in elementary through middle school provide the foundation for studying high-school-level algebra. The Star Math™ Record Book Student Details page provides an Algebra Readiness Indicator to help teachers identify student progress through these foundational skills.

Research has identified the progression of skills needed for algebra readiness. The following table identifies the Core Progress Math skills associated with these algebra readiness skills. This list can help you identify the grade-level skills a student may need to practice to achieve expected grade-level progress.

**Note:** An asterisk (\*) following a skill indicates that the skill develops fluency. Practicing the skill throughout the school year helps students achieve speed and accuracy.

Grade 3
Assess the reasonableness of the answer to a 2-step problem using any of the four operations
Compare two fractions with the same denominator using any method
Compare two fractions with the same numerator using any method
Demonstrate that the area of a rectangle is the same using tiling or multiplying side lengths
Demonstrate the distributive property using tiling in a rectangular array
Describe the total number of objects in a rectangular array using multiplication
Determine the unknown in a division equation
Determine the unknown in a multiplication equation
Estimate a liquid volume in liters
Estimate the mass of an object using grams or kilograms
Explain arithmetic patterns using properties of operations
Explain why two fractions are equivalent using a visual fraction model
Express a whole number as a fraction or a fraction as a whole number
Find an unknown side length of a polygon given the perimeter and the other side lengths to solve a real-world or mathematical problem
Find the area of a rectangle by multiplying side lengths
Find the area of a rectangle by multiplying side lengths to solve a problem

## Grade 3 continued

Find the area of a rectangle with whole-number side lengths by tiling

Find the area of a rectilinear figure by decomposing it into non-overlapping rectangles and adding the areas of the non-overlapping parts

Find the area of a rectilinear figure in a real-world problem by decomposing it into non-overlapping rectangles and adding the areas of the non-overlapping parts

Find the perimeter of a polygon given the side lengths to solve a real-world problem

Fluently add within 1000\*

Fluently divide within 100, using basic facts\*

Fluently multiply within 100, using basic facts\*

Fluently subtract within 1000\*

Generate simple equivalent fractions

Identify arithmetic patterns

Interpret a multiplication fact as the sum of equal groups

Interpret the whole-number quotient of a division fact as a partitioning into equal shares

Justify the result of a comparison of two fractions with like numerators or denominators

Know basic multiplication facts within 100

Measure a liquid volume in liters

Measure a time interval in minutes

Measure length to the nearest half inch or quarter inch

Measure the mass of an object using grams or kilograms

Multiply whole numbers within 100 using strategies based on properties of operations

Recognize a non-unit fraction as the sum of unit fractions on a number line

Recognize area as an attribute of plane figures

Recognize equivalent fractions

Recognize that a comparison of fractions is valid only when the fractions refer to the same whole

Recognize that equally partitioning the interval between 0 and 1 on a number line creates unit fractions

Relate a fraction to a point on a number line

Relate area to the number of square units

Represent a 2-step problem using an equation with a letter standing for the unknown

## Grade 3 continued

Represent a unit fraction on a number line

Represent a whole-number product as a rectangular area in mathematical reasoning

Represent the distributive property in mathematical reasoning using area models

Select and use an appropriate measurement tool

Solve a 1-step problem involving mass or volume

Solve a 2-step problem with whole numbers using any of the four operations

Solve a problem involving addition or subtraction of time intervals in minutes

Solve a problem within 100 involving arrays

Solve a problem within 100 involving equal groups

Solve a problem within 100 involving measurement quantities

Tell and write time to the nearest minute, including indication of a.m. and p.m.

Understand division as an unknown factor problem

Understand how the unit square is defined

Understand that area can be measured using unit squares

Understand the size of a fraction

Understand the structure of a fraction

Understand what it means for two fractions to be equivalent

## Grade 4

Add or subtract fractions with like denominators

Add or subtract fractions with like denominators to solve a problem

Add two fractions with unlike denominators of 10 and 100 using equivalent fractions

Assess the reasonableness of a whole number answer to a multi-step problem

Classify a 2-dimensional figure

Compare two decimals through hundredths using standard symbols

Compare two fractions with different numerators and denominators using standard symbols

Compare two whole numbers up to 1,000,000

Convert a fraction in tenths to an equivalent fraction in hundredths

Decompose a fraction into a sum of fractions with the same denominator in more than one way

Distinguish between multiplicative and additive comparisons

Estimate the solution to a multiplication or division problem

Explain why two fractions are equivalent by relating visual fraction models to multiplying the numerator and denominator of a fraction by the same number

Express a fraction with a denominator of 10 or 100 as a decimal

Find a common denominator of two fractions

Generate equivalent fractions by multiplying the numerator and denominator of a fraction by the same number

Interpret a multiplication equation as a comparison

Interpret the remainder in a multi-step word problem

Justify the result of a comparison of two decimals through hundredths

Justify the result of a comparison of two fractions with unlike numerators and denominators

Know basic geometric elements: point, line, line segment, ray, angles (right, acute, obtuse), a set of perpendicular lines, and a set of parallel lines

Multiply a fraction by a whole number

Multiply a fraction by a whole number to solve a problem

Multiply or divide in a given situation involving multiplicative comparison

Read and write a whole number in expanded form up to 1,000,000

Read and write a whole number in standard form up to 1,000,000

## Grade 4 continued

Read and write a whole number in word form up to 1,000,000

Recognize equivalent fractions by identifying common factors

Recognize that in a multi-digit whole number, a digit in any place represents ten times what it represents in the place to its right

Represent a situation using an equation with a letter standing for the unknown quantity

Represent a verbal statement of multiplicative comparison as a multiplication equation

Rewrite an expression involving multiplication of a fraction and a whole number

Round a decimal number to a specified place through hundredths

Round a whole number within 1,000,000 to a specified place

Show that one or more fraction decompositions are equivalent to a given fraction

Solve a multi-step problem with whole numbers involving the four operations

Solve a problem using the area or perimeter formulas for rectangles

Solve an addition or subtraction problem to find an unknown angle measure on a diagram

Understand a fraction as a multiple of a unit fraction

Understand a fraction as a sum of unit fractions

Understand a multiple of a fraction as a multiple of a unit fraction

Understand addition of fractions as joining parts referring to the same whole

Understand subtraction of fractions as separating parts referring to the same whole

## Grade 5

Add decimals through hundredths using one of various strategies

Add decimals through hundredths using pictures or concrete models

Add or subtract fractions or mixed numbers with unlike denominators

Add or subtract mixed numbers with like denominators

Assess the reasonableness of an answer to an addition or subtraction problem involving fractions

Compare the size of a product of two fractions to the size of one factor based on the size of the other factor

Compare two decimals through thousandths

Define elements of the coordinate system

Demonstrate that the volume of a right rectangular prism is the same using either packing or multiplying edge lengths

Demonstrate the reasoning used in a division problem with a dividend of up to four digits and a 2-digit divisor

Demonstrate the reasoning used in solving a multiplication or division problem involving decimals through hundredths

Demonstrate the reasoning used in solving an addition or subtraction problem involving decimals through hundredths

Divide a unit fraction by a nonzero whole number

Divide a unit fraction by a nonzero whole number to solve a problem

Divide a whole number by a unit fraction

Divide a whole number by a unit fraction to solve a problem

Divide a whole number of up to four digits by a 2-digit whole number using one of various strategies

Divide decimals through hundredths using one of various strategies

Divide whole numbers to solve a problem, leading to an answer in the form of a fraction or a mixed number

Estimate a sum or difference of two fractions

Estimate the solution to a problem

Explain the pattern in the number of zeros of a product when multiplying numbers by powers of 10

Explain the pattern in the placement of the decimal point when multiplying or dividing decimals by powers of 10

Explain the result of multiplying a number by a fraction equal to 1, less than 1, or greater than 1

## Grade 5 continued

Find the volume of a right rectangular prism by counting unit cubes

Find the volume of a right rectangular prism by multiplying edge lengths

Find the volume of a right rectangular prism to solve a problem, using a formula

Find the volume of a solid figure composed of right rectangular prisms by decomposing it into two non-overlapping parts and adding the volumes of the non-overlapping parts

Fluently multiply multi-digit whole numbers

Graph a point in the first quadrant of the coordinate plane

Interpret a fraction as division of the numerator by the denominator

Interpret coordinate values of points within a given context

Interpret division of a unit fraction by a nonzero whole number

Interpret division of a whole number by a unit fraction

Interpret the product of a fraction and a fraction or whole number as parts of a partition or a sequence of operations

Model multiplication of fractions by finding the area of a rectangle using tiling

Multiply a fraction by a fraction

Multiply decimals through hundredths using one of various strategies

Multiply decimals through hundredths using pictures or concrete models

Multiply fractional side lengths of a rectangle to find its area

Multiply fractions and mixed numbers in a given situation

Read and write a decimal through thousandths in any form

Recognize that in a multi-digit number, a digit in any place represents  $\frac{1}{10}$  of what it represents in the place to its left

Recognize volume as an attribute of solid figures

Relate a fraction product to a rectangular area model

Represent powers of 10 using whole-number exponents

Solve a problem by finding the volume of a solid figure composed of right rectangular prisms through decomposing it into two non-overlapping parts and adding the volumes of the non-overlapping parts

Solve a problem by graphing a point in the first quadrant of the coordinate plane

## Grade 5 continued

Find the volume of a right rectangular prism by counting unit cubes

Find the volume of a right rectangular prism by multiplying edge lengths

Find the volume of a right rectangular prism to solve a problem, using a formula

Find the volume of a solid figure composed of right rectangular prisms by decomposing it into two non-overlapping parts and adding the volumes of the non-overlapping parts

Fluently multiply multi-digit whole numbers

Graph a point in the first quadrant of the coordinate plane



## Grade 6

Convert measurement units using ratios

Describe a ratio relationship between two quantities

Determine a unit rate

Divide mixed numbers or fractions

Evaluate a numerical expression involving whole-number exponents

Evaluate an expression for specific values of its variables

Express the sum of two whole numbers in factored form using the distributive property

Find missing values in a ratio table

Find the area of polygons including special quadrilaterals composed of triangles and/or rectangles

Find the areas of parallelograms and triangles, including right triangles

Find the greatest common factor of whole numbers less than or equal to 100

Find the least common multiple of two whole numbers less than or equal to 12

Fluently add and subtract multi-digit decimals using the standard algorithm

Fluently divide multi-digit whole numbers

Fluently multiply and divide multi-digit decimals using the standard algorithm

Graph in the coordinate plane the values of a ratio table

Identify attributes of a 3-dimensional shape

Identify parts of an expression using mathematical terms

Identify the relationship between two variables using graphs and tables

Interpret an inequality between two rational numbers in context

Interpret the meaning of a positive number, a negative number, or zero in a given situation

Know and be able to apply the fact that the opposite of the opposite of a number is the original number

Know the difference between the ordering of rational numbers and their magnitudes

Model a situation involving division of a fraction by a fraction

Plot coordinates to form a polygon on the coordinate plane

Plot rational numbers on a horizontal or vertical number line

Recognize a constraint or condition in a mathematical problem

## Grade 6 continued

Recognize a percent of a quantity as a part per 100

Recognize a percent of a quantity as a part per 100 in a given situation

Recognize that dividing by a rational number is the same as multiplying by its reciprocal

Recognize that opposite numbers are located on opposite sides of zero on a number line

Relate a graph or a table showing the relationship between two variables to an equation

Relate a statement of inequality to the relative positions of two rational numbers on a number line

Relate an input-output table to equivalent ratios

Relate an ordered pair to its location on a coordinate plane

Relate the locations of two ordered pairs that differ only by signs

Represent a quantity using a positive or negative number in a given situation

Represent the solution of an inequality of the form  $x > c$  or  $x < c$  on a number line diagram

Solve a problem by evaluating an expression or formula for specific values of its variables

Solve a problem by finding a side length of a polygon on the coordinate plane

Solve a problem involving an equation of the form  $x + p = q$  or  $px = q$  with nonnegative rational numbers

Solve a problem involving division of a fraction by a fraction

Solve a problem involving parts, wholes, and percentages

Solve a problem using a formula to find the volume of a right rectangular prism with fractional-edge lengths

Solve a problem using absolute value to describe magnitude

Solve a real-world or mathematical problem by graphing points in all four quadrants

Solve a unit rate problem

Substitute to determine whether a given number is a solution to an equation or an inequality

Understand ordering of rational numbers

Understand signs of numbers in ordered pairs as indicating locations in the quadrants of the coordinate plane

Understand that a rational number is represented by a point on the number line

Understand that a variable can represent an unknown number or any number in a specified set

Understand that positive and negative numbers are used to represent quantities having opposite directions or values

## Grade 6 continued

Understand the absolute value of a rational number as its distance from zero on a number line

Understand the concept of a ratio

Understand the concept of a unit rate

Understand what constitutes a solution in an equation or inequality with variables

Use tables to compare ratios in a given situation

View one or more parts of an expression as a single entity

Write a numerical expression involving whole-number exponents

Write an equation of the form  $x + p = q$  or  $px = q$  to represent a situation involving nonnegative rational numbers

Write an equation with two variables to express one quantity in terms of another in a given situation

Write an expression containing variables to model a situation

Write an expression using one or more operations that involves variables

Write an inequality of the form  $x > c$  or  $x < c$  to represent a constraint or condition

Write an inequality to describe the relationship between two rational numbers

Write equivalent expressions using variables and properties of operations

## Grade 7

Add integers

Add or subtract to simplify a linear expression with rational coefficients

Add rational numbers

Assess the reasonableness of an answer to a multi-step problem involving rational numbers

Compare fractions, decimals, and percents

Compare how to solve a word problem algebraically to solving it arithmetically

Compute the unit rate associated with a ratio of fractions

Convert between rational numbers in any form

Describe a real-world situation using a linear inequality

Describe a situation in which opposite quantities combine to make zero

Determine if the decimal form of a rational number terminates or repeats

Determine the distance between two rational numbers on a number line

Determine the measure of an unknown angle in a geometric figure

Divide integers

Divide rational numbers

Expand a linear expression with rational coefficients

Factor a linear expression with rational coefficients

Fluently solve equations of the form  $px + q = r$  or  $p(x + q) = r$

Graph the solution set of an inequality involving rational numbers

Identify a common irrational number

Identify the constant of proportionality

Illustrate the concept of additive inverse on a number line

Interpret the meaning of an ordered pair on a graph that shows a proportional relationship in a given situation

Multiply integers

Multiply rational numbers

Solve a multi-step percent problem involving a proportional relationship

Solve a multi-step problem involving rational numbers

## Grade 7 continued

Solve a multi-step ratio problem involving a proportional relationship

Solve a problem involving a scale drawing of a geometric figure

Solve a problem involving the surface area or volume of a 3-dimensional object

Solve a problem leading to a 2-step linear inequality involving rational numbers

Solve a problem with rational numbers involving any of the four operations

Subtract integers

Subtract rational numbers

Understand  $p + q$  as a number located a distance  $|q|$  from  $p$  on a number line

Understand subtraction of rational numbers as adding the additive inverse

Understand that different forms of an expression can show how its various quantities are related

Understand that multiplication is extended from fractions to rational numbers

Understand that the division of two integers always results in a rational number, provided that the divisor is not zero

Understand that the negative sign in a rational number may apply to the numerator or the denominator

Understand the rules for multiplying signed numbers

Use the product of two rational numbers to describe a real-world situation

Use the quotient of two rational numbers to describe a real-world situation

## Grade 8

Compare the relative size of two numbers written in scientific notation

Compare two linear functions each represented in a different way

Compare two proportional relationships each represented in a different way

Convert between standard decimal notation and scientific notation

Demonstrate similarity between two figures by listing a sequence of transformations

Derive the equation  $y = mx + b$  for a line intercepting the vertical axis at  $b$

Derive the equation  $y = mx$  for a line through the origin

Describe a functional relationship that is modeled by a graph

Determine if a relation is a function

Determine if the variables in a situation are in a proportional or linear non-proportional relationship given a table, a graph, or an equation

Determine the rate of change or initial value of a function from a description of a relationship or from two  $(x, y)$  values

Estimate the solution to a system of two linear equations by graphing

Evaluate the cube root of a perfect cube up to 1000

Evaluate the roots of a perfect square up to 144

Explain why the slope of a line is the same between any two distinct points using similar triangles

Find an unknown side length of a right triangle, using the Pythagorean theorem

Find the distance between two points, using the Pythagorean theorem

Generate an equivalent expression using properties of integer exponents

Give an example of a linear equation in one variable with one solution, infinitely many solutions, or no solution

Graph a proportional relationship

Identify a function that is not linear

Identify the number of solutions for a linear equation in one variable

Interpret a unit rate as the slope of a graph

Interpret scientific notation that has been generated by technology

Interpret the rate of change or initial value of a linear function in terms of the situation it models

Know the properties of integer exponents

## Grade 8 continued

Perform operations with numbers written in scientific notation

Recognize the equation  $y = mx + b$  as defining a linear function whose graph is a straight line

Represent a quantity using scientific notation and units of the appropriate size

Sketch a graph to model a function given a verbal description

Solve a linear equation with rational coefficients

Solve a problem by finding an unknown side length of a right triangle, using the Pythagorean theorem

Solve a problem leading to two linear equations in two variables

Solve a real-world or mathematical problem involving the volume of a cone, cylinder, or sphere

Solve a simple quadratic or cubic equation

Solve a simple system of two linear equations by inspection

Solve a system of two linear equations in two variables algebraically

Understand similarity through transformations

Understand that a function is a rule that assigns to each input exactly one output

Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs

Understand that the graph of a function is the set of ordered pairs consisting of an input and the corresponding output

Use scientific notation to estimate a very large or a very small quantity

Write a function to model a linear relationship between two quantities